Enhanced Nonlinear Companding Scheme for Reducing PAPR of OFDM Systems

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Abstract—A new companding scheme for reducing the peakto-average power ratio (PAPR) of orthogonal frequency-division multiplexing (OFDM) systems is proposed in this study. It proceeds from speech signal processing similar to the earliest μ -law companding (MC) model. The proposed scheme compands (compresses and expands) the amplitudes of OFDM signals to a maximum of 1 V. Besides significantly reducing the PAPR, the proposed technique is also able to function as a limiter, thus reducing the system complexity and limiting the amplitudes of OFDM symbols to a unity maximum voltage, which does not exist in other companding PAPR techniques. Over frequency-selective fading channels with frequency domain equalization and using minimum mean square error (MMSE) to minimize the noise overhead, the proposed technique outperforms four other companding schemes over light and severe fading conditions. Finally, we demonstrate that PAPR reduction using companding can dispense with corresponding decompanding scheme at the receiver as it amplifies the distortion noise, thereby reducing the bit error ratio performance and increasing the receiver complexity. We investigate the out-of-band interference of the proposed scheme and also show that it outperforms the other existing techniques by up to 5 dB.

Index Terms—Limiter, nonlinear companding, orthogonal frequency-division multiplexing (OFDM), out-of-band interference (OBI), peak-to-average power ratio (PAPR), power amplifier (PA).

I. INTRODUCTION

O RTHOGONAL frequency-division multiplexing (OFDM) is a multicarrier scheme for processing communication signals. It has the advantage of high spectral efficiency due to narrow frequencies of the OFDM scheme and robustness over multipath fading channels due to increased symbol time. However, its major drawback is the high peakto-average power ratio (PAPR) problem. The high PAPR may drive the power amplifier (PA) of a communication system

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to operate near the saturation region. Although nonlinear PAs need large input backoff for linear amplification, increasing the backoff can be used to mitigate the problem. Such solution incurs higher power consumption, thus reducing the efficiency of PAs [1].

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Presently, different techniques have been proposed to alleviate the PAPR problem in OFDM systems. These can be broadly grouped into signal distortion techniques, multiple signaling and probabilistic techniques, and coding techniques [2]. Some of these techniques can be performed before or after multicarrier modulation. Based on these two criteria, the three groups of PAPR reduction schemes [2] can further be classified into two groups [3], [4], namely signal scrambling and signal amplitude distortion (SAD) techniques. Examples of PAPR reduction schemes before OFDM modulation include partial transmit sequence [5], selective mapping [6], [7], and coding [8]. Furthermore, clipping [9]–[11] and companding [12] techniques are applied after OFDM modulation. Other OFDM design kernels, such as wavelets [13], possess low PAPR than the conventional OFDM scheme. While clipping expands the system processing time due to (2m+1) fast Fourier transform (FFT)/inverse FFT (IFFT) operations (m is the number of clipping/filtering iterations), companding increases the receiver complexity due to decompanding of companded signals.

This paper proposes a nonlinear PAPR reduction technique based on SAD, which does not require decompanding at the receiver, thus relaxing the complexity of using companding techniques. It achieves companding and also limits the amplitude of OFDM symbols to a unit-voltage. Specifically, we introduce in this paper a novel nonlinear companding PAPR reduction technique that can limit both the input and output power levels to a maximum of one (unit-voltage) amplitude. We will refer to this new model as an amplitude-limiting companding (ALC) scheme. Such a property makes the proposed scheme more attractive than other previously proposed PAPR reduction schemes. The PAPR and bit error ratio (BER) results of the proposed scheme will be compared with four other widely used companding techniques, such as μ -law companding (MC), log-based MC (LMC), hyperbolic arcsin companding (HASC), and exponential companding (EC) schemes [14]–[17].

Companding has potentials to be applied in the candidate waveforms of future 5G standard [18], [19], namely generalized frequency-division multiplexing (GFDM). GFDM is a form of filter-bank multicarrier technique for 5G waveform candidates that deploy standard OFDM structure [18]–[21].

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A. Related Work and Summary of Main Contributions

Companding (an example of SAD PAPR reduction) generally refers to compressing and expanding some OFDM signal amplitudes [14], [15]. It operates on the amplitudes of OFDM signal only without any impact on the phase. The foremost companding model reduces the PAPR of OFDM systems using μ -law [14] and was later explored in other studies [2], [12], [22]–[25]. The MC technique is a nonlinear process that involves distorting the amplitudes of some lower OFDM signal amplitudes without impacting the higher amplitude signals, which leads to the limited performance of the scheme. However, the ideal companding scheme requires distorting both high and low amplitude signals. Consequently, the seminal work of [15] describes a general model for companding OFDM signals, which involves distorting both high and low amplitude signals. Companding has been shown to possess lower in-band distortion noise than clipping [26] and can be applied in power line communication systems [27].

Since the EC method was proposed [15], there are limited novelties afterward on effective companding models (see [23], [24], [28]–[30]). Only recently, Peng et al. [31] suggested imposing a choice constraint on the default Rayleigh probability density function (PDF) of OFDM signal amplitudes for PAPR reduction. It follows that there are two main models for PAPR reduction using the companding scheme, namely first, using the transformation identity described in [15] by comparing the cumulative distribution function (CDF) of unmodified OFDM signal amplitudes and that of a choice uniform distribution model, and second, by imposing a choice constraint on the Rayleigh PDF of OFDM signal amplitudes knowing that $\int_{0}^{c} f_{|x|}(x) dx = 1$ where c is a desired cutoff point [31]. Based on these two criteria, especially on the cutoff point, different piecewise companding models [23], [28], [29], [32] have been proposed. Recently, this idea of conversion to uniform distribution has been extended to clipping [10], which is also a post-OFDM PAPR reduction scheme just like companding [25], [26]. There are also the linear companding transforms [33]; however, these are not treated in this study as they are outside the scope of our present study.

One problem with previous companding models include the abrupt scaling of input and output signal power levels. In particular, the earliest MC [14] unfairly expands the power level of low amplitude signals thereby leading to unfairly better BER than the unmodified signals [34]. To solve this usually requires additional scaling to normalize the power level [15], [34]. First, new MC-based models that overcome this problem can be found in [16] and [35]. Second, most of the PAPR reduction techniques were not discussed over fading channels. Third, these PAPR reduction schemes require decompanding at the receiver, which complicates the receiver system. Noting all these complexities, first, we propose the use of a PAPR reduction model that scales both the input and output powers of the OFDM signal to a desired power level by default. Second, the general system model is tested over multipath fading channel and the results are seen to be more robust than all other widely used PAPR models in the literature. Third, we demonstrate that the proposed model can be operated without correspondingly decompanding the transmitted signal due to the fact that the decompanding tool expands both the noise power and also the receiver complexity.

As our proposed model can limit the signal to a desired power level, an additional requirement/tool (e.g., limiter) to scale the power of the signal to a desired power level is not required in the proposed PAPR reduction model. Finally, we derive the decompanding transform to recover the companded signal at the transmitter.

When compared with four other widely known companding techniques, namely MC, LMC, HASC, and EC, the PAPR and out-of-band interference (OBI) of the proposed ALC outperforms those four earlier techniques including the uncompanded signals. Due to the amplitude distortions suffered by the OFDM signals during PAPR reduction, the in-band noise generated by the companding process causes degradation in the BER performances of OFDM systems. Thus, we evaluate the OFDM signals when transmitted over frequency fading channels over light and severe fading conditions. It was observed that the proposed technique is more robust than other techniques over frequency fading channels with minimum mean square error (MMSE) equalization performed in frequency domain.

The remaining parts of this paper is organized as follows. Section II introduces the system model and describes the nonlinear companding transform (NCT). The results and discussion are presented in Section III. Finally, conclusions are drawn in Section IV.

II. GENERAL SYSTEM MODEL

Consider some N-point randomly generated data symbols, $\boldsymbol{b}(t) \ \forall t = 1, \dots, T$. Thus, $\boldsymbol{b}(t)$ is the t^{th} symbol vector of the form $\boldsymbol{b}(t) = [b_0, b_1, b_2, \dots, b_{N-1}]^T$, where $[\cdot]^T$ represents transpose. The symbols can be processed using the quadrature phase-shift keying (QPSK) or quadrature amplitude modulation modulator and then passed through an OFDM modulator to generate some time-domain OFDM symbol as

$$\boldsymbol{x}(n) = \frac{1}{\sqrt{LN}} \sum_{k=0}^{LN-1} \boldsymbol{X}(k) e^{j2\pi \frac{kn}{LN}} \quad \forall n = 0, 1, \dots, LN-1$$
⁽¹⁾

where $\boldsymbol{x}(n)$ is the time-domain signal and L is the oversampling factor. This factor must satisfy $L \ge 4$ [36]. Since the OFDM symbols are complex, we define their amplitudes as

$$|\boldsymbol{x}(n)| = \sqrt{\boldsymbol{x}_r(n)^2 + \boldsymbol{x}_i(n)^2} \quad \forall n = 0, 1, \dots, LN - 1$$
 (2)

where $\boldsymbol{x}_r(n)$ and $\boldsymbol{x}_i(n)$ are from $\boldsymbol{x}(n) = \boldsymbol{x}_r(n) + j\boldsymbol{x}_i(n)$ and $j = \sqrt{-1}$. From the central limit theorem, the real and imaginary OFDM parts have asymptotically independent and identical Gaussian distribution for any sufficiently large number of subcarriers [3]. In other words, the amplitudes ($|\boldsymbol{x}(n)|$) follow a Rayleigh distribution as [3]

$$f_{|\boldsymbol{x}(n)|}(x_0) = \frac{x_0^2}{\sigma^2} \exp\left(-\frac{x_0^2}{2\sigma^2}\right) \quad \forall n = 0, 1, \dots, LN - 1$$
(3)

where x_0 is the discrete-time envelope of $\boldsymbol{x}(n)$ and σ^2 is the variance.

A. Calculating the PAPR

To estimate the amplitudes of OFDM symbols exceeding a desired amplitude target T_0 , when processed using a PAPR reduction technique [for instance using an NCT $\mathcal{F}(x)$], the PAPR metric is used. For the original OFDM symbols x(n), the PAPR can be calculated as

$$PAPR = \frac{\max_{n=0,1,\dots,LN-1} \left(|x(n)|^2 \right)}{\frac{1}{LN} \sum_{n=0}^{LN-1} \left(|x(n)|^2 \right)}.$$
 (4)

The CDF C_X , which is related to the complementary CDF (CCDF) as $CC_X = 1 - C_X$, is usually used to measure the PAPR technique performance [16] and is given by

$$C_X = \Pr\{|\boldsymbol{x}(n)| \le T_0\}$$

= 1 - exp $\left(-\frac{x_0^2}{\sigma^2}\right) \quad \forall x_0 \ge 0$ (5)

where C_X basically measures the probability that the amplitude of the OFDM symbol exceeds a target threshold, T_0 . Considering all points, i.e., $n = 0, 1, \dots, LN - 1$, the CDF can be rewritten as

$$C_X (\boldsymbol{x}(n)) = \Pr \{ |\boldsymbol{x}(0)| \le T_0 \} \times \Pr \{ |\boldsymbol{x}(1)| \le T_0 \}$$
$$\times \Pr \{ |\boldsymbol{x}(2)| \le T_0 \} \cdots \Pr \{ |\boldsymbol{x}(LN-1)| \le T_0 \}$$
$$= \left(1 - \exp\left(-\frac{x_0^2}{\sigma^2}\right) \right)^{LN}.$$
(6)

Meanwhile, if the companding function $\mathcal{F}(\boldsymbol{x}(n)) = \boldsymbol{y}(n)$, the decompanding function at the receiver is given by $\hat{x}(n) =$ $\mathcal{F}^{-1}(\mathcal{F}(\boldsymbol{x}(n)))$. Then, the PAPR of the companded symbols in this case can be described from the CDF as follows

$$C_Y \left(\mathcal{F}(\boldsymbol{x}(n)) \right) = \Pr \left\{ \left| \mathcal{F}(\boldsymbol{x}(n)) \right| \le T_0 \right\}$$
$$= \Pr \left\{ \left| \boldsymbol{y}(n) \right| \le T_0 \right\}$$
(7)

so that the CCDF metric can be written as $CC_Y (\mathcal{F}(\boldsymbol{x}(n))) =$ $1 - C_Y \left(\mathcal{F}(\boldsymbol{x}(n)) \right).$

B. Proposed NCT

Function $\mathcal{F}(\cdot)$ is itself an NCT that compresses/expands the amplitudes of the higher energy signals to a maximum/minimum of a 1-volt, respectively, which leads to significant PAPR reduction. Then, the degree of the distortion with respect to the uncompanded input symbols will influence the BER performance. If $x_{\text{lin}} = \mathcal{G} \{x\} = a_1 x + b_1$ is the output of linearly companded OFDM signal [3], then for NCTs, for example in MC, the function $\log(1 + \mu)$ expands the amplitudes of the lower energy symbols [34] only. If an NCT, namely $x_{n \text{ lin}} = \mathcal{F} \{x\} = a_2 x^{\alpha} + b_2$ when $1 \le \alpha \le \infty$, then $|x_{n \ln}(n)|^2$ increases as $\alpha \to \infty$ and decreases (in fact, it approaches a constant) as $\frac{1}{\alpha} \rightarrow 0$, where x is the OFDM symbol; this is also upheld in [35]. Based on these,

we propose

$$U = \left(1 + \left(\frac{v}{|x(n)|}\right)^{1/\alpha}\right)^{-\alpha} \tag{8}$$

where v is used to control the input amplitude of the symbol, $\alpha = \frac{1}{s}$ and $s \in \mathbb{R}^+$. Similar to MC motivated by speech processing, (8) has been motivated by the nonlinear behaviour of systems described in [37] and both linear companding transform and NCT discussed in [38]. Considering the phase of the signal [4] (i.e., sgn(x)) and the fact that the output amplitude can be limited to a designated voltage level, say M, then [37]

$$y(n) = \mathcal{F}(x(n)) = M \times \operatorname{sgn}(x(n)) \times U$$
(9)

where $\operatorname{sgn}(x) = \frac{x}{|x|} \forall x = x_r + jx_i$ and M is the output limiting value. To ensure that y(n) dissipates equivalent power as the uncompanded symbol (for fair comparison), we weigh the result in (9) as

$$x_{c}(n) = \beta \times \mathcal{F}(x(n))$$
(10)

where β is a scaling factor that ensures equal power dissipation with the uncompanded signals x(n). Define

$$\mathbb{E}\left\{\left|x(n)\right|^{2}\right\} = \int_{0}^{\infty} x^{2} f_{|x(n)|}\left(x\right) dx,$$
(11)

where $f_{|x(n)|}$ is the PDF of x(n) usually expressed as in (3), then

$$\beta = \left\{ \frac{\mathbb{E}\left\{ |y(n)|^2 \right\}}{\mathbb{E}\left\{ |x(n)|^2 \right\}} \right\}^{\frac{1}{2}}$$
(12)

where $\mathbb{E}\left\{\cdot\right\}$ is the expectation value operator. For fair comparisons with other PAPR reduction schemes, we also extended the use of β normalization parameter in (12) to the other four companding techniques to ensure equal energy dissipation with the uncompanded OFDM signals. There are 2LN computational operations in the proposed ALC scheme, 7N in MC, 13N in EC, and 7N in LMC; however, there are 18LN operations in HASC. In fact, most MC-based models have similar computational costs (see [14], [16], [35]). Although nonlinear in operation, the proposed ALC technique is simpler and more efficient than HASC, EC, and LMC (see [14]-[17]).

We show in Fig. 1 the effects of input and output limiting voltage parameters on the signal amplitudes. When the output voltage is M = 1, all the signal amplitudes are limited to 1 V and when increased to M = 4, the output voltage shows 4 V. To ensure a maximum of 1-V output signal, we set M = 1 in all subsequent examples. Also, the PAPR varying parameter ν limits the input signal according to choice parameter. When small, e.g., $\nu = 0.2$, the proposed ALC model distorts the amplitudes by expansion and when large, e.g., $\nu = 1$, our proposed ALC technique distorts the amplitude by compression, however, without exceeding the maximum output voltage M.

Since $\mathcal{F}(\cdot)$ can limit all amplitudes to ± 1 , then $\mathcal{F}(\cdot)$ provides the advantages of a compander and a limiter. From (9), M determines the amplitude of the output signal, v is the input limiting value, and s determines the shape of the companded

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Fig. 1. Effects of input voltage and output voltage on the performance of the ALC scheme on signal amplitudes.

symbol. Since the maximum amplitude of communication signals are usually normalized to unity, we set $0 < M \le 1$. For amplitudes approximable to 1 volt, we suggest $0.5 \le M \le 1$. Next, parameter v determines the PAPR output value and also directly impacts the error vector magnitude (EVM) of the OFDM symbols (see [39]). Similar to the M variable, we also suggest $0.5 \le v \le 1$ for amplitudes approximable to 1 volt. There exists poorer BER with further reductions in v, for example, v = 0.1; however, the PAPR reaches minimum possible. Over an additive white Gaussian noise (AWGN) channel with mean zero and variance σ_z^2 , the received signal becomes

$$\boldsymbol{r}(n) = \boldsymbol{x}_c(n) + \boldsymbol{z}(n)$$

= $\mathcal{F}(\boldsymbol{x}(n)) + \boldsymbol{z}(n)$ (13)

where z(n) is the AWGN. Let $\gamma = \frac{\mathbb{E}\{|x_c(n)|^2\}}{\mathbb{E}\{|z(n)|^2\}}$ be the received signal-to-noise ratio (SNR). Here, it is worthy to note that any further distortion, by v, will increase the background noise thereby reducing the output SNR and, thus, lowering the BER performance.

Two factors will influence the EVM: One is the degree of distortions to the input symbols, which can be controlled in this study by setting s > 0 and v > 0. The other is correctly recovering the transmitted symbols by the decompanding function, $\mathcal{F}^{-1}(\mathcal{F}(x(n)))$, at the receiver. Consequently, the decompanding function of the companded OFDM symbol at the receiver can be given by

$$\mathcal{F}^{-1}\left(\mathcal{F}(x\left(n\right))\right) = \frac{v}{\mathcal{B}}\operatorname{sgn}(y\left(n\right))$$
$$\mathcal{B} = \left(\left(\frac{M}{|y\left(n\right)|}\right)^{s} - 1\right)^{\frac{1}{s}}.$$
 (14)

proof: See the Appendix for the proof.

We can now rewrite (13) as

$$\hat{\boldsymbol{x}}(n) = \mathcal{F}^{-1} \left(\boldsymbol{r}\left(n\right)\right)$$
$$= \mathcal{F}^{-1} \left(\mathcal{F}(\boldsymbol{x}\left(n\right)\right)\right) + \mathcal{F}^{-1} \left(\boldsymbol{z}\left(n\right)\right)$$
$$= \boldsymbol{x}(n) + \mathcal{F}^{-1} \left(\boldsymbol{z}\left(n\right)\right)$$
(15)

where $\mathcal{F}^{-1}(\cdot)$ is the decompanding transform. Both $\mathcal{F}(x)$ and $\mathcal{F}^{-1}(\mathcal{F}(x))$ are NCTs that are based on v and M.

From Bussgang theory [4], [40], the output of the companded signals can be expressed as

$$\boldsymbol{x}_{c}(n) = \mathcal{F}\left(\boldsymbol{x}(n)\right) = \rho \boldsymbol{x}(n) + \boldsymbol{d}(n)$$
(16)

where ρ is the attenuation factor that determines the output signal amplitude and d(n) is the distortion noise after $\mathcal{F}(\boldsymbol{x}(n))$ operation. Substituting (16) into (13) gives

$$r(n) = \rho \boldsymbol{x}(n) + \boldsymbol{d}(n) + \boldsymbol{z}(n)$$
$$= \rho \boldsymbol{x}(n) + \boldsymbol{z}_a(n)$$
(17a)

where the total noise at the receiver can be expressed as

$$\boldsymbol{z}_a(n) = \boldsymbol{d}(n) + \boldsymbol{z}(n). \tag{17b}$$

At the receiver, using (15) in (17a), the output decompanded signal can be expressed as

$$\hat{\boldsymbol{x}}(n) = \mathcal{F}^{-1} \left(\boldsymbol{r} \left(n \right) \right)$$

$$= \boldsymbol{x}(n) - \frac{\boldsymbol{d}(n)}{\rho} + \frac{\boldsymbol{z} \left(n \right)}{\rho}$$

$$= \boldsymbol{x}(n) + \boldsymbol{z}_{b}(n)$$
(18a)

where

$$\boldsymbol{z}_{b}(n) = \frac{1}{\rho} \boldsymbol{z}(n) - \frac{\boldsymbol{d}(n)}{\rho}.$$
 (18b)

Now, assuming that $\mathcal{F}^{-1}(\mathbf{r}(n))$ is absent (in other words, no decompanding is applied) at the receiver, clearly only (17a) is received with ρ impacting the amplitude of $\mathbf{x}(n)$ and $\mathbf{z}_a(n)$. Comparing (18b) and (17b), the noise $(\mathbf{z}_a(n) \text{ and } \mathbf{z}_b(n))$ are impacted by $\mathbf{d}(n) + \mathbf{z}(n)$ and $\frac{1}{\rho}\mathbf{z}(n) - \frac{\mathbf{d}(n)}{\rho}$, respectively. Since the model in (9) offers both the input and output amplitudes, $\rho = \nu$; this implies that as $\nu \to 1$, then only the distortion noise $\mathbf{d}(n)$ impacts $\mathbf{z}(n)$ as in (17b). However, with decompanding at the receiver as in (18b), the distortion noise is amplified by ρ as in $\frac{\mathbf{d}(n)}{\rho}$, which diminishes the received signal power (including γ) and further reduces the BER performance. We shall exemplify the impacts decompanding and no decompanding at the receiver in Section III-C.

C. Impacts of Companding Transform on the Signals

The degrees of impacts of amplitude distortions on the input symbols during companding are demonstrated in Fig. 2. For the sake of comparison, we also include the behaviors of the LMC, HASC, and EC schemes. Comparing the original and companded symbols using the proposed ALC companding model in Fig. 2, it can be observed that all the amplitudes of the input symbols are impacted. Unlike the earlier methods (e.g., MC), the



Fig. 2. Comparison of original and companded symbols for different methods (M = 1 and v = 1).



Fig. 3. Nonlinear behavior of proposed compander when M = 1 in comparison with four other widely used companding models.

ALC model compands all the amplitudes of the input symbols toward 1-volt. This will lead to significant PAPR reduction as will be shown later. Notice that LMC, HASC, and EC schemes compand all amplitudes, but not targeting a maximum/minimum of ± 1 V.

D. Behavior of the Proposed Nonlinear Compander

In this section, we compare the companding performance of the proposed transform with EC, MC, HASC, and LMC. In Fig. 3, it can be seen that the MC scheme expands the amplitudes of low amplitude signals only. On the other hand, the proposed ALC scheme compands all the amplitudes to a maximum of M-volts (M = 1) and a minimum of ν -volts ($\nu = 1, 0.55$). Considering the other transforms, LMC largely expands the amplitudes of the OFDM symbols, thus increasing the energy of the output signals which leads to lower BER performance while EC moderately distorts all the amplitudes, but larger than the proposed scheme. Worst of all is the HASC scheme, which does not alter the amplitudes of lower energy signals; in fact, of all moderately higher energy signals, this will lead to better BER performance.

For any chosen value of s, ν must be carefully selected not to tradeoff the PAPR for the BER or vice versa. Meanwhile, to achieve much lower PAPR for the proposed ALC technique, $\nu \rightarrow 0$. However, s must be kept reasonably large, for example, $1 \le s \le \infty$. In Table I, we provide a summary of a comparative performance table for all the PAPR reduction models considered in this study.

E. Transmission and Evaluation of the Companded Signal Over Fading Channel

The BER performances of PAPR reduction schemes over fading channels are usually scarcely reported. Meanwhile, some authors have exemplified the use of partial transmit sequence and OFDM/time division multiplexing (TDM) over fading channels including the effects of nonlinear PAs [41], [42]. Due to the difficulty in modeling PAs, PAs are then modeled as typical frequency-selective fading channel model examples in studying PAPR reduction problems [43]. In another study, the filter-bank multicarrier system typical of the future 5G standard [18]-[20] was studied for PAPR reduction over such fading channel instance [44]. Both [44] and [41] show that over fading channels, multicarrier systems suffer severe degradation in BER performance with irreducible error at lower BER measures. These depend on the severity of the fading in the channel and certain PAPR reduction schemes can perform better than others over different fading channel conditions (see Section III-B).

To start with, we model the system as over a Rayleigh multipath fading channel with impulse response $h(\tau)$ and the channel transfer function H(f), where

$$H(f) \underset{\text{FFT}}{\overset{\text{IFFT}}{\rightleftharpoons}} h(\tau).$$
(19)

Generally, channel modeling may involve perfect channel state information (CSI) or imperfect CSI. In time division duplexing, the CSI is simplified due to the reciprocity of the channel; however, in frequency division duplexing, a feedback mechanism is required to update the transmitter with CSI observed at the receiver. This is usually encumbered by first, the noise in the CSI sent to the transmitter causing mismatch; and second, the CSI is usually outdated due to finite delay associated with feedback [45], [46]. To relax these complexities, we assume that the CSI is perfectly known at the receiver. At the receiver, the received signal (after the removal of cyclic prefix) can be expressed as

$$Y(f) = H(f)X_c(f) + Z(f) \quad \forall f = 0, 1, \dots, LN - 1 \quad (20)$$

where $X_c(f)$ and Z(f) are the transformed companded signal and the AWGN, respectively, in frequency domain. Given the frequency-selective fading channel, the new SNR can be

 TABLE I

 COMPARATIVE ANALYSES OF DIFFERENT COMPANDING PAPR REDUCTION MODELS

| Companding model | Shape parameter | Power level normalization | Output amplitude parameter | Expands weak signal | Compress stronger signals | Limits input/output power level |
|---------------------|--------------------|------------------------------|----------------------------|------------------------|------------------------------|------------------------------------|
| EC | d > 0 | Inbuilt | No | When d is | Always | No |
| | | | | large | | |
| MC | $\mu > 0$ | Required | No | Always | No | No |
| LMC | $\mu, a, b > 0$ | Inbuilt | No | Always | Always | No |
| ALC | s > 0 | Inbuilt | Yes, $M = 1$ | Always | Always | Yes, $M = 1, \nu = 1$ |
| HASC | $c, k_1 k_2 > 0$ | Inbuilt | No | Slightly | Always | No |

expressed as

$$\gamma(X_c, H) = \frac{\mathbb{E}\left\{|H(f)X_c(f)|^2\right\}}{\mathbb{E}\left\{|Z(f)|^2\right\}} = \frac{\sigma_{x,H}^2}{\sigma_Z^2} \qquad (21)$$

where $\sigma_{x,H}^2$ is the received signal power over fading channel, $H \sim \mathcal{N}(\mu_H, \sigma_{x,H}^2)$ and σ_Z^2 is from $Z \sim \mathcal{N}(0, \sigma_Z^2)$.

At the receiver, the received signal Y(f) is then decompanded to recover the estimate of the original transmitted signal before PAPR mitigation processing. We also similarly performed decompanding for other companding models (EC, LMC, HASC, and MC) to which the proposed ALC is compared with. From (21), the BER performance depends on σ_Z^2 . To minimize its effect and also compensate for the effect of H, we construct an MMSE filter, which has been widely adopted in noise-sensitive communication systems [47]. Using the MMSE filter, the received signal can be expressed as

$$\hat{X}_c = \mathcal{G}_{\text{MMSE}}\left(f\right)Y(f) \tag{22}$$

where the f index shows the frequency indices of the channel coefficient and $\mathcal{G}_{\text{MMSE}}(f)$ represents the frequency domain MMSE filter, which can be expressed as [42]

$$\mathcal{G}_{\text{MMSE}}(f) = \frac{H^*(f)}{|H^*(f)|^2 + \left(\frac{E_s}{N_0}\right)^{-1}}$$
(23)

where E_s/N_0 is the output SNR. Since the MMSE scheme has potential to improve the BER performance by reducing the noise, the output received signal estimate can be expressed as

$$\hat{X}_{c} = \mathcal{G}_{\text{MMSE}}(f) Y(f)$$
(24a)
$$= X_{c} + \frac{H^{*}(f)}{|H^{*}(f)|^{2} + \left(\frac{E_{s}}{N_{0}}\right)^{-1}} Z(f)$$
$$= X_{c} + \hat{Z}$$
(24b)

where

$$\hat{Z} = \frac{H^*(f)}{|H^*(f)|^2 + \left(\frac{E_s}{N_0}\right)^{-1}} Z(f)$$
(24c)

from which the characteristic covariance matrix can be used to discuss the output SNR and BER performance. In the case of AWGN-only channel, the companded signal was impacted by the noise from the companding process and the AWGN; however, over fading channel, the BER of the signal will further be impacted by $\mathcal{G}_{\text{MMSE}}(f)$. Examples of these results have been reported involving the use of PAPR and MMSE in [41] and [42]; thus, we adopt these in the results in Section III-B.

III. RESULTS AND DISCUSSIONS

In the simulations, we generate N = 128 random input symbols and mapped these using QPSK modulation, then normalized the signals to ensure a maximum output power of 1. The resulting symbols are oversampled L = 4-times so that an oversized IFFT/FFT of 512 points is used to generate OFDM timedomain signals as shown in (1). To protect the signals over fading channels, cyclic prefix that has 25% length of the time-domain signal is added. Next, we estimate the PAPR for the original symbols before applying the proposed ALC PAPR reduction scheme. Later, we measure the PAPR of the proposed ALC PAPR reduction scheme to assess the level of reduction achieved compared to the original OFDM symbols. Subsequently, the PAPR reduced OFDM signals are passed through the channel and AWGN is added. At the receiver, we apply the inverse ALC operation to decompand the companded signals. Then, we removed the cyclic prefix and performed the forward FFT to transform the received signal into frequency domain. In the frequency domain, we applied the MMSE equalization described in (24a) and performed inverse oversampling. The received signals were demodulated using QPSK before bit error estimation. We present the results in Sections III-A and III-B. These processes were then repeated for HASC, LMC, and EC techniques for comparisons. In all, we adopted s = 60 and M = 1.

A. Performance Evaluation of the Proposed Scheme Over AWGN-Only Channels

Fig. 4 shows the results of the proposed ALC scheme and the other four companding schemes under consideration. Although all the companding schemes reduce the PAPR, some outperform others. However, upon comparing the proposed ALC scheme with LMC at 10^{-5} CCDF, it is found that although the proposed scheme outperforms all other (LMC, HASC, MC, and EC) schemes at 10^{-5} CCDF, the proposed ALC scheme is specifically better than LMC by up to 3.3 dB when $\nu = 0.7$. When v = 1, the proposed scheme also reduces the PAPR of the original symbol from 12 dB to 4.6 dB and outperforms three of the other schemes (EC, HASC, and LMC), but slightly worse than MC and LMC at 10^{-5} CCDF.

In addition, the proposed technique achieves the lowest BER among all the existing schemes under investigation, but slightly worse than the uncompanded signals as it is found in Fig. 5 when v = 1. This can be explained on the premise that our proposed



Fig. 4. PAPR comparison of the proposed method with other companding techniques (when M = 1, N = 128, L = 4) over AWGN fading channel.



Fig. 5. BER performance of different companding techniques with the proposed method (M = 1, N = 128, L = 4).

ALC scheme induces the least distortion noise to the signals when companded than other companding schemes. Specifically, at 10^{-4} BER, the proposed scheme gains 5 dB in SNR better than MC, 2 dB better than LMC, 1 dB better than EC, and slightly better than HASC.

Recall that in Section II-D, we showed that LMC largely expands the amplitudes of the OFDM symbols, thus increasing the energy of the output signals, which leads to lower BER performance better than MC; meanwhile, the proposed ALC scheme moderately expands the energy of the lower amplitude signals and compresses the amplitudes of high energy signals, which was instrumental to both good PAPR and BER performances. Also in Fig. 5, when v = 0.7, in other words, when the attenuation is increased, the amplitudes of the symbols is then largely distorted leading to more distortion noise and, thus, lowering the BER performance. Notwithstanding, the proposed ALC scheme outperforms MC, LMC, and HASC at low BER measure.



Fig. 6. PSD comparisons of the different companding PAPR reduction techniques including the uncompanded OFDM signals.



Fig. 7. PAPR comparison of the proposed method with other companding techniques (when M = 1, N = 512, L = 4).

Finally, we explore OBI and also plot in Fig. 6, the power spectral density (PSD) for the five companding techniques including that of the original OFDM symbols. Clearly, the proposed ALC technique produces 5.64, 3.53, 3.49, and 3.66 dB OBI lower than the MC, LMC, EC, and HASC techniques, respectively, including 3.1 dB better than the uncompanded signals.

It is worth noting that it is possible to completely reduce the PAPR further using the proposed model by further reducing the PAPR determining value ν ; however, this will further diminish the BER performance. To further illustrate the superior performances of our results, we demonstrate the performance of the proposed scheme with the four other companding schemes under discussion as shown in Figs. 7 and 8 for PAPR and BER performances when N is increased. As in Figs. 4 and 5, our proposed ALC scheme outperforms the other schemes upholding the superiority of our model both when N is large or small.



Fig. 8. BER performance of different companding techniques with the proposed ALC method (M = 1, N = 512, L = 4) over the AWGN fading channel.



Fig. 9. Channel description and behavior in both time and frequency domains.

B. Performance Evaluation of the Proposed Companding Scheme Over Frequency-Selective Fading Channels With MMSE

Although not commonly reported, we examine the BER performance of the proposed companding transform over the frequency-selective fading channel. The resulting companded signal is linearly convolved with the channel impulse response in time domain and AWGN is added. The AWGN noise impacts the in-band distortions already incurred by the signals during compression and expansion of the amplitudes. At the receiver, the received signal is decompanded and then demodulated using an OFDM demodulator. This is done by the removal of cyclic prefix followed by performing the FFT on the received signal, which transforms the signal into frequency domain and the results are shown in (20). In Fig. 9, we depict the impulse and channel responses of the channel model used.

Now, with the received signal Y(f) in frequency domain, and using perfect knowledge of CSI at the receiver, frequency



Fig. 10. BER performance evaluation of the proposed companding scheme over frequency-selective fading channel with MMSE equalization method in comparison with other companding schemes, namely MC, LMC, EC, and HASC [number of channel taps (nTaps = 2 and 5), L = 4, N = 128].

domain equalization is performed as in (22) and the results are shown in Fig. 10. In Fig. 10, the BER performances of the five companding techniques under study are compared over a frequency-selective fading channel with 2 and 5 channel taps, respectively. It is found that the proposed ALC technique outperforms the other four techniques under investigation in terms of BER.

Companding involves deliberately distorting the amplitudes of OFDM signals. This amplitude distortion creates in-band distortion noise that impacts the EVMs of the originally transmitted data symbols. EVM measures the deviation of the processed signals (e.g., amplitude distorted symbols) from the original constellation position, which in turn gives information into the possible BER performance of the system. Although a PAPR technique that significantly reduces PAPR of OFDM signals is attractive, the BER must also be preserved. At significantly low BER in Fig. 10, say 10^{-5} , the ALC companded OFDM signals slightly deteriorated as the channels' taps increased from 2 to 5. On the other hand, the ALC scheme performed similarly as the uncompanded signals until the significantly low BER is achieved. This shows its robustness over frequency-selective fading channels after being impacted by fading, for nTap = 2, by the in-band distortion noise due to amplitudes companding (ρ) . Now, compared to EC, LMC, HASC, and MC schemes, the proposed ALC scheme outperformed all. The trend of performance of the proposed technique has been derived from the fact that it compands OFDM signals to a preset amplitude threshold allowing uniform spread of the channel fading thus leading to lower BER. Also, when the MMSE equalization filter impacts the distortion noise and AWGN at the receiver, higher distortion noise leads to poorer BER performance. When increased to 5 taps, the EC, LMC, HASC, and MC schemes were severely impaired at lower BER measures than the proposed scheme.

In Fig. 11, we demonstrate the performance of the proposed scheme over fading channels when the attenuation increases and

 $\nu = 0.5$

 $\nu = 0.7$

= 1

Original

nTap=10



25

SNR [dB]

30

35

40

45

50

nTap=2

nTap=2, 5 and 10 for the

20

uncompanded OFDM signals

15

10⁰

10

10⁻²

10⁻³

10-4

10-5

10⁻⁶

0

5

nTap=5

10

Bit Error Ratio



Fig. 12. BER performance evaluation companded signals with and without decompanding for different attenuation weights over the AWGN-only channel.

under severe fading conditions (e.g., nTaps = 2, 5, and 10). It is found that increasing the attenuation produced slight impairments compared to increasing the fading channel conditions, nTaps = 10. Thus, we infer that despite the PAPR reduction ability provided by the proposed ALC scheme, it is also robust over severe fading conditions.

C. Performance Evaluation of Decompanded Systems and Undecompanded Systems

We showed in Section II-B that decompanding at receiver amplifies the noise (both distortion noise and AWGN). In this section, we show the performances of the systems with and without decompanding at the receiver for fading and nonfading channels.



Fig. 13. BER performance evaluation companded signals with and without decompanding for different attenuation weights over frequency-selective fading channel with AWGN.

From Fig. 12, the results show that decompanding degrades the BER performance at the receiver. In addition, increasing the attenuation weight further increases the distortion noise, which is amplified if decompanded. Over fading channels as shown in Fig. 13, the equalization filter amplifies the distortion with and without the decompanding.

However, the impact becomes more significant when decompanding is applied at the receiver. Thus, companding PAPR reduction schemes for reducing the PAPR of OFDM signals should be implemented without decompanding as it both degrades the BER performance of the system and also increases the receiver complexity, expands processing time, and consumes system power.

IV. CONCLUSION

In this paper, we presented a new companding technique that has the ability to reduce PAPR as well as limit the peak amplitudes of OFDM symbols to a unit-voltage. Using simulation results, the proposed method was shown to outperform four other widely used companding schemes such as MC, HASC, LMC, and EC methods in terms of PAPR, OBI, and BER metrics over AWGN channel. Based on the desired output performance of the OFDM system, the PAPR can be completely eliminated by further resetting the PAPR determining parameter ν in the proposed model to values smaller than 0.5 V. Over fading channels, it is found that the proposed technique significantly outperforms EC, LMC, HASC, and MC schemes at all channel tap instances, thus making it more suitable for applications over practicable real-life channel environments. In fact, at less severe fading channel conditions such as the Rician channel or line-of-sight transmissions, it can be conjectured that the proposed companding scheme will perform as similar to dispensing without PAPR reduction techniques leading to low complexity systems. It is further shown that companding PAPR schemes can be deployed without correspondingly decompanding the received signals at

the receiver as the decompanding process amplifies the distortion noise by the attenuation weight, thus leading to poorer BER performances. Also, operating companding schemes in only OFDM system transmitters can as well reduce the receiver complexity and eliminate expending the required system power to process the decompanding process.

APPENDIX

Define $\operatorname{sgn}(y) = \frac{y}{|y|}$ and let $\operatorname{sgn}(x) \approx \operatorname{sgn}(y)$, then rearranging (9), we obtain

$$\frac{y}{\operatorname{sgn}(x)} = \frac{M}{\left(1 + \left(\frac{v}{|x|}\right)^{s}\right)^{\frac{1}{s}}}$$
$$\left(1 + \left(\frac{v}{|x|}\right)^{s}\right)^{\frac{1}{s}} = \frac{M}{|y|}$$
$$\left(\frac{v}{|x|}\right)^{s} = \left(\frac{M}{|y|}\right)^{s} - 1 \Longrightarrow |x| = \frac{v}{\mathcal{B}} \qquad (25)$$

where $\mathcal{B} = ((\frac{M}{|y|})^s - 1)^{\frac{1}{s}}$. We have assumed that $\operatorname{sgn}(x) \approx \operatorname{sgn}(y)$ because companding transform only operates on the amplitudes of OFDM signals; however, it does not impact the phase of the signal which $\operatorname{sgn}(x)$ and $\operatorname{sgn}(y)$ represent. Multiplying it by $\operatorname{sgn}(x)$

$$x = \operatorname{sgn}\left(y\right)\frac{v}{\mathcal{B}}\tag{26}$$

so that [where $sgn(x) \approx sgn(y)$]

$$\mathcal{F}^{-1}\left(\mathcal{F}(x)\right) = \operatorname{sgn}\left(y\right)\frac{v}{\mathcal{B}}$$
$$\mathcal{B} = \left(\left(\frac{M}{|y|}\right)^{s} - 1\right)^{\frac{1}{s}}.$$
 (27)

This is the end of the proof.

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